

where

$$g_2 = \frac{E_1}{E_2} \left[ \frac{k_2^2 + 1}{k_2^2 - 1} + \nu + \frac{M_2 f_3(r_1)}{\beta_1} + E_2 \frac{G_2}{r_1} + g_{m4}(r_1) \right] + \frac{k_1^2 + 1}{k_1^2 - 1} - \nu \quad (66)$$

Similarly,  $q_1$  is found if  $p$  is taken as zero; i. e.,

$$q_1 = \frac{E_1 \Delta T (\alpha_1 - k_2 \alpha_2)}{g_2} \quad (67)$$

Formulating the range in hoop stress  $(\sigma_\theta)_r$  at the bore (Equation (56)) and using the definition  $\alpha_r \sigma_1 = (\sigma_\theta)_r$ , we get the following expression for  $p/\sigma_1$ :

$$\frac{p}{\sigma_1} = \frac{2\alpha_r (k_1^2 - 1)^2 g_2}{\left[ g_2 (k_1^4 - 1) - 4k_1^2 \right]} \quad (68)$$

[Equation (68) is identical in form to Equation (58).]

The pressure-to-strength ratio  $p/\sigma_1$  is plotted in Figure 58. Comparing this figure with Figure 45 for the multiring container with  $\alpha_r = 0.5$ , it is evident that both containers have the same limit  $p/\sigma_1 \rightarrow 1$  for large wall ratios. However,  $\alpha_r = 0.5$  is possible only if  $\alpha_m \leq 0$  as shown in Figure 42. Actually,  $\alpha_m = +0.5$  is likely in the pin-segment container if  $\alpha_r = 0.5$  because any interference is expected to be lost in taking up slack between pins and holes. In this case, then,  $\alpha_r = 0.5$  would mean only one cycle life whereas  $\alpha_r = 0.5$  means  $10^4$  to  $10^5$  cycles life in the multiring container. If this assembly problem could be eliminated by careful machining and selective fitting of pins, then theoretically with sufficient compressive prestress, the  $p/\sigma_1$  ratio of the pin-segment container could be made to approach that of the multiring container.

Since no prestress has been assumed for the pin-segment container,  $\alpha_r = \alpha_m = 0.35$  for  $10^4$  to  $10^5$  cycles as shown by Figure 42. For  $\alpha_r = 0.35$ , it is found that  $p/\sigma_1$  is limited to 0.7 at best. Therefore, the maximum pressure in the pin-segment container is  $p = 0.7 (300,000) = 210,000$  psi for  $10^4$  to  $10^5$  cycles life.

The stresses in the segments have not yet been considered. High stresses develop around the pin holes. These too limit the pressure in the pin-segment container. Analysis of the stresses in the segments is described in Appendix I. For the purpose of estimating stresses in the segments the interface pressure  $p_1$  is needed. Therefore, plots of  $p_1/p$  are provided in Figure 59. It is evident that the interface pressure  $p_1$  is appreciably less than the bore pressure  $p$  especially for large  $k_1$  and small  $k_2$ .

The pins are analyzed in Appendix II. In order to carry the pressure loading  $p_1$ , it is found that the pin-to-segment-diameter ratio must be

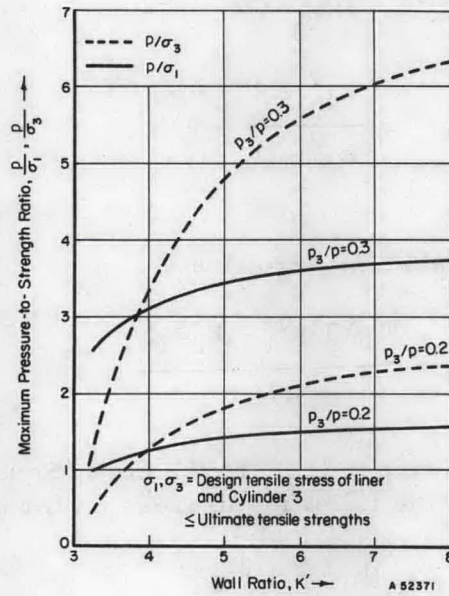


FIGURE 57. EFFECT OF SUPPORT PRESSURE,  $p_3$ , ON BORE PRESSURE,  $p$ , CAPABILITY FOR THE RING-FLUID-SEGMENT CONTAINER

$$\alpha_r = 0.5, \alpha_m = -0.5$$

$$k_1 = 1.5, k_2 = 2.0.$$

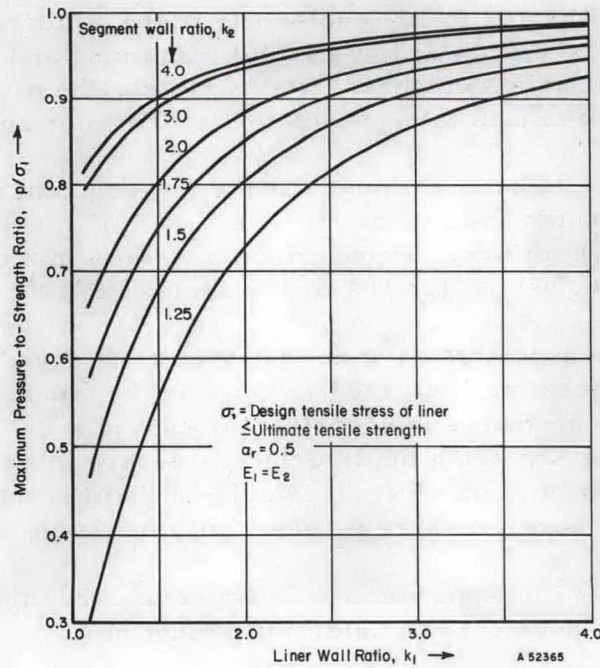


FIGURE 58. MAXIMUM PRESSURE-TO-STRENGTH RATIO,  $p/\sigma_1$ , FOR THE PIN-SEGMENT CONTAINER